

We study topic-based communication between agents and its strategic version

(Arbitrary) Partial Communication

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1. Partial (Topic-Based) Communication

Let $M = \langle W, R, V \rangle$ be a model with $R_G := \bigcap_{k \in G} R_k$, $\sim_\varphi^M := ([\varphi]^M \times [\varphi]^M) \cup ([\neg\varphi]^M \times [\neg\varphi]^M)$, $R^{S:\chi!}_i := R_i \cap (R_S \cup \sim_\chi^M)$, and $M_{S:\chi!} := \langle W, R^{S:\chi!}, V \rangle$. The semantics of $\mathcal{L}_{S:\chi!}$ is as follows:

$$\begin{aligned} (M, w) \Vdash D_G \varphi & \text{ iff } \forall u \in W : R_G w u \text{ implies } (M, u) \Vdash \varphi \\ (M, w) \Vdash [S:\chi!] \varphi & \text{ iff } (M_{S:\chi!}, w) \Vdash \varphi \end{aligned}$$

Results. (1) Axiomatisation of $\mathcal{L}_{S:\chi!}$ is **sound and complete** via reduction axioms.

(2) Model Checking is in P.

(3) $\mathcal{L}_{S:\chi!}$ is as **expressive as public announcement logic**, but their **update expressivities** are **incomparable**.

2. Arbitrary Partial Communication

The language $\mathcal{L}_{S:\chi!}^*$ extends $\mathcal{L}_{S:\chi!}$ with a modality $[S:*\!]$.

$$(M, w) \Vdash [S:*\!] \varphi \text{ iff } \forall \chi \in \mathcal{L} : (M_{S:\chi!}, w) \Vdash \varphi$$

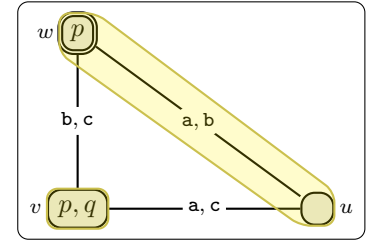
Results. (1) An **infinitary** axiomatisation of $\mathcal{L}_{S:\chi!}^*$ is **sound and complete**.

(2) Model Checking is PSPACE-complete.

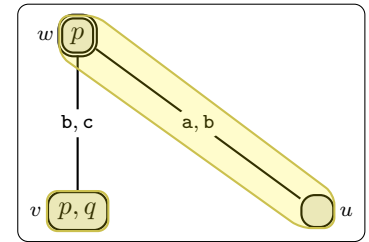
(3) $\mathcal{L}_{S:\chi!}^*$ is **incomparable** to *arbitrary public announcement logic*.

Examples

Initial model M with highlighted $\sim_{p \rightarrow \neg q}^M$



Example 1: agents b and c communicate on topic $p \rightarrow \neg q$ with the resulting model $M_{\{b,c\}:p \rightarrow \neg q!}$:



Example 2: all agents communicate on topic $p \rightarrow \neg q$ with the resulting model $M_{\{a,b,c\}:p \rightarrow \neg q!}$:

